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# Majoron dark matter from a spontaneous inverse seesaw model

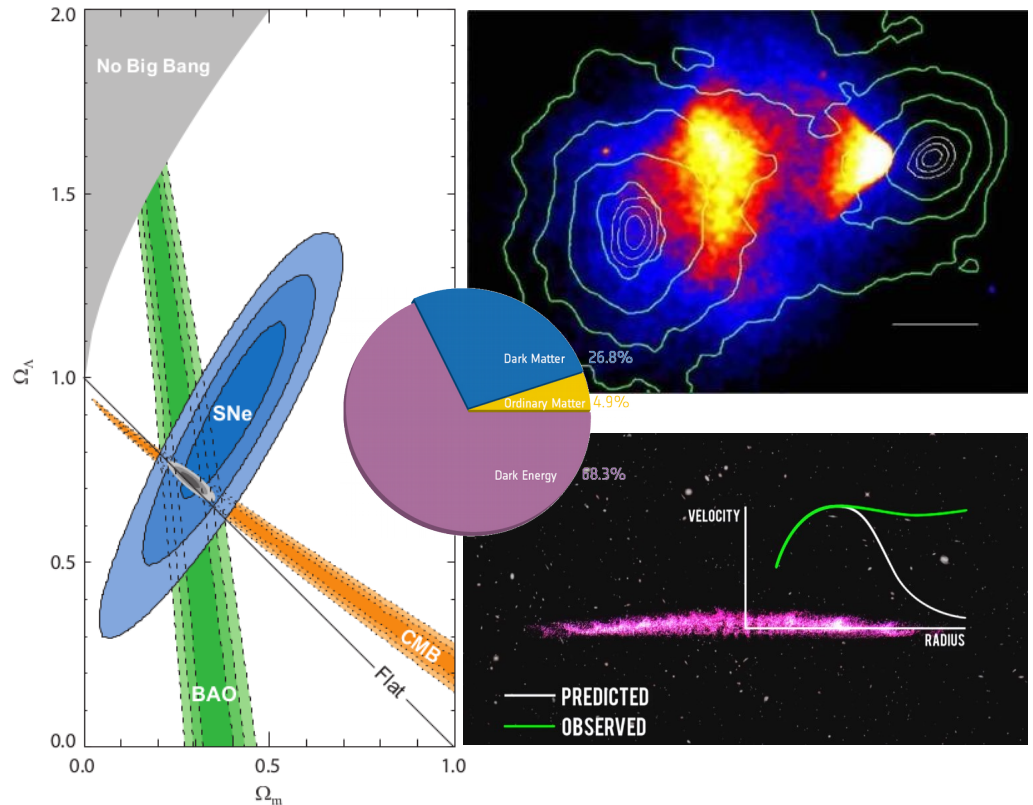
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Instituto de Física Corpuscular UVEG/CSIC

In collaboration with N. Rojas and F. Gonzales-Canales – arxiv:1703.03416

Seminar ULB PhysTH – May 5, 2017

# Motivation

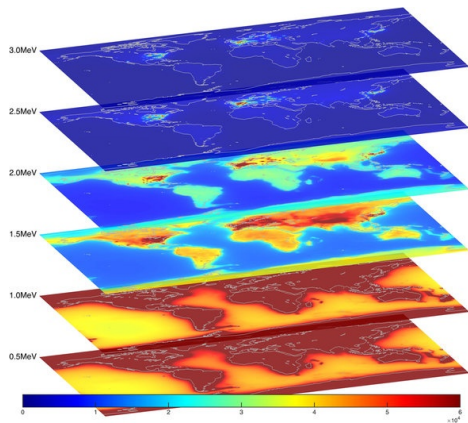
Majoron DM models provide a tantalizing connection between Dark Matter and Neutrinos



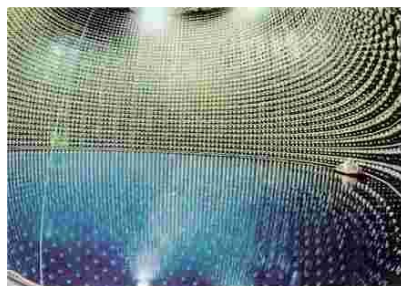
# This talk



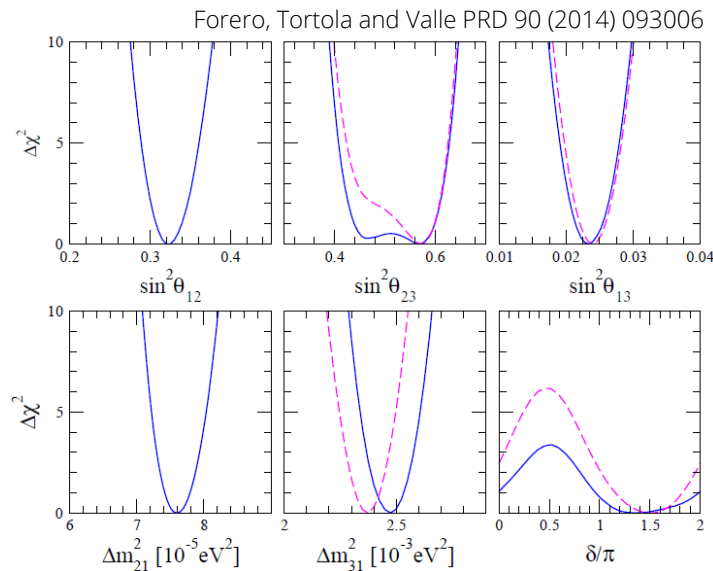
# Neutrinos



AGM2015: Antineutrino Global Map 2015



Super-K:  
Neutrinos in the Sun



The **SM** predicts zero neutrino mass

**Beyond SM** physics is required to explain  
mass spectrum and mixing angles

# Neutrino mass mechanisms

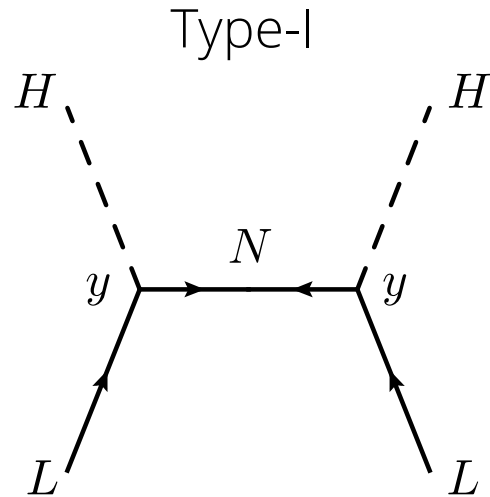
A large fraction of the models uses the 5-dim Weinberg operator to generate *majorana* neutrino masses

$$\mathcal{O}_{5ij} \propto (L_i H)^T (L_j H)$$

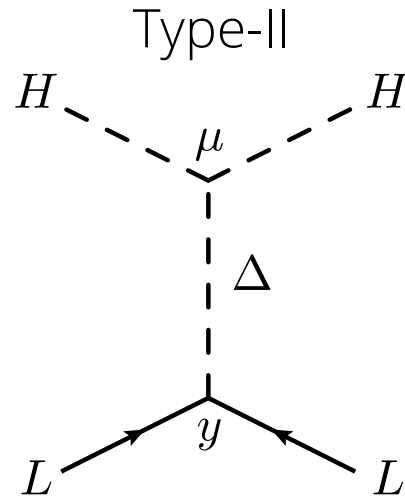
This operator breaks lepton number in 2 units

# Neutrino mass mechanisms

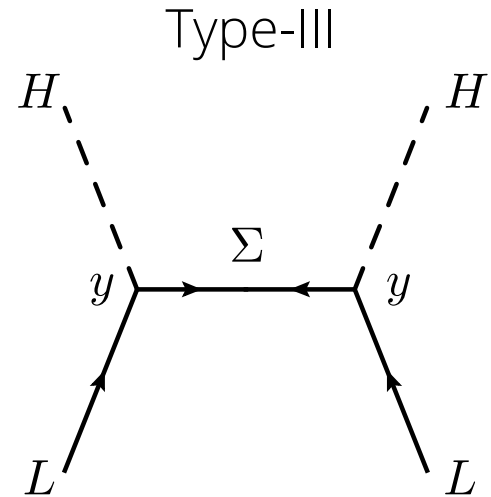
The commonly known schemes are **see-saw mechanisms**



$$m_\nu \propto \frac{v^2 y^2}{M_N}$$



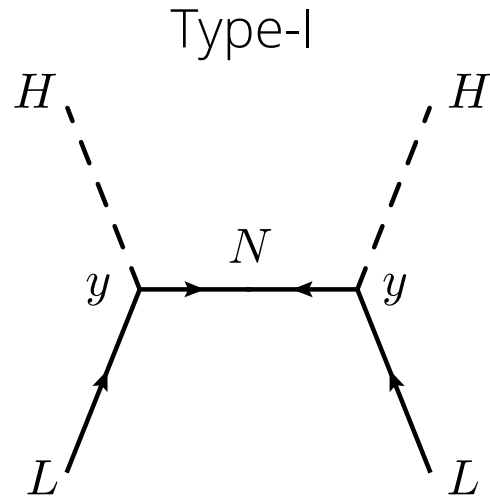
$$m_\nu \propto \frac{v^2 y \mu}{M_\Delta^2}$$



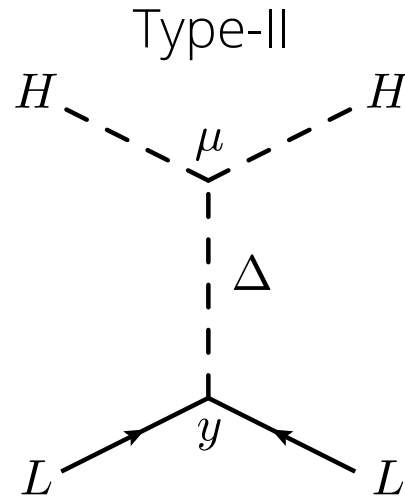
$$m_\nu \propto \frac{v^2 y^2}{M_\Sigma}$$

# Neutrino mass mechanisms

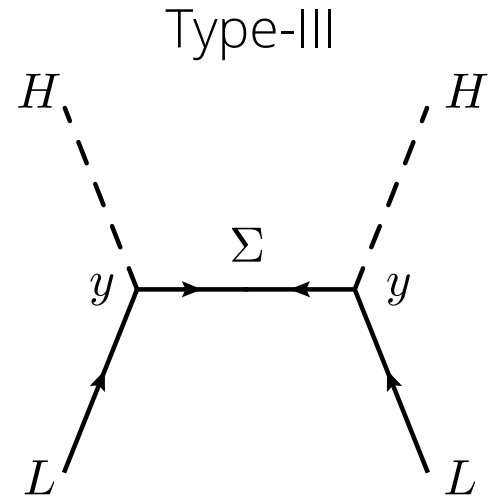
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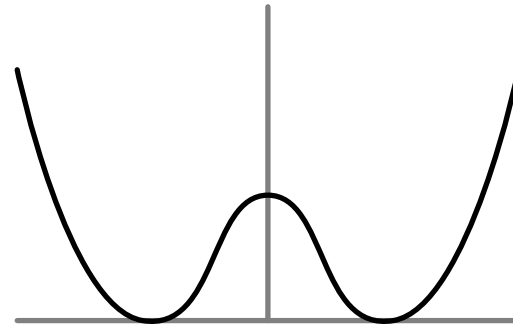


$$m_\nu \propto \frac{v^2 y^2}{M_\Sigma}$$

# Enters the Majoron

The Type-I seesaw can be generated by the spontaneous breaking of the  $U(1)$  lepton number symmetry

$$S = \frac{v_S + \sigma + iJ}{\sqrt{2}}$$



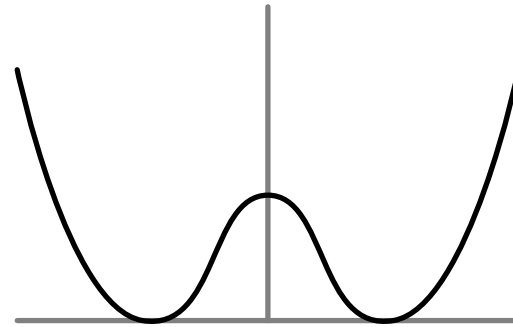
$$\mathcal{L} \supset -y_L \bar{L} H N^c - \frac{y_S}{2} S \bar{N}^c N + h.c.$$



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$\begin{matrix} -1 & 0 & 1 \\ 2 & -1 & -1 \end{matrix}$

# Enters the Majoron

$$m_D = \frac{y_L v_H}{\sqrt{2}}$$

$$M_N = \frac{y_S v_S}{\sqrt{2}}$$

After the SSB, we get the Type-I seesaw

$$\mathcal{L} \supset -m_D \bar{\nu}_L N^c - \frac{M_N}{2} \overline{N^c} N + h.c.$$

and 2 scalars:  $\sigma$  and  $J$

$$m_\sigma \simeq v_S \quad m_J = 0$$

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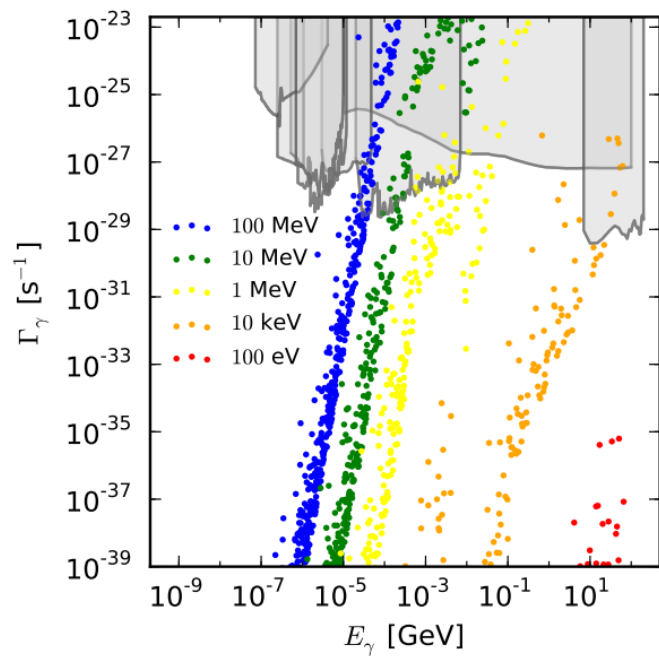
$$\mathcal{L} \supset -m_D \bar{\nu}_L N^c - \frac{M_N}{2} \overline{N^c} N + h.c.$$

and 2 scalars:  $\sigma$  and  $J$   DM candidate

$$m_\sigma \simeq v_S \quad m_J = 0$$

# Majoron as DM (pros)

- Neutral
- Weakly coupled to the SM
- Long lived



$$\Gamma_{J \rightarrow \nu\nu} = \frac{m_J}{32\pi} \frac{\sum_i (m_i^\nu)^2}{2v_1^2}$$
$$\Gamma_{J \rightarrow \gamma\gamma} = \frac{\alpha^2 m_J^3}{64\pi^3} \left| \sum_f N_f Q_f^2 \frac{2v_3^2}{v_2^2 v_1} (-2T_3^f) \frac{m_J^2}{12m_f^2} \right|^2$$

# Majoron as DM (cons)

$$m_J = 0 \quad ! ! ! !$$

... but global symmetries are not protected under gravity effects

Therefore

$$m_J \neq 0$$

... and the majoron DM is just a pseudo Nambu-Goldstone boson

# Majoron as DM (our fixing)

What defines a **majoron DM**?

- It is a (pseudo)scalar
- It is part of the neutrino mass mechanism
- Its signature is the decay into neutrinos
- It is massive

# ~~Spontaneous~~ Inverse seesaw

The **standard** inverse seesaw

$$\mu \ll m_D \ll M$$

$$\mathcal{L} = -\frac{1}{2} n_L^T C \mathcal{M} n_L + h.c.$$

$$n_L^T = (\nu_L, N_1^c, N_2)$$

$$\mathcal{M} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix}$$

# ~~Spontaneous~~ Inverse seesaw

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$$\mathcal{M} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M \\ 0 & M^T & \mu \end{pmatrix}$$

Lepton number  
violating term



# ~~Spontaneous~~ Inverse seesaw

The **standard** inverse seesaw

$$\mu \ll m_D \ll M$$

Active neutrinos

$$m_\nu = \left( \frac{m_D}{M} \right)^2 \mu$$

Heavy neutrinos

$$m_{\mathcal{N}'} = M - \frac{m_D^2}{M} + \frac{\mu}{2}$$
$$m_{\mathcal{N}} = M - \frac{m_D^2}{M} - \frac{\mu}{2}$$

# ~~Spontaneous~~ Inverse seesaw

The **standard** inverse seesaw

$$\mu \ll m_D \ll M$$

Some numerology:

$$M \sim 100 \text{ TeV} \quad m_D \sim 10 \text{ GeV} \quad \mu \sim 10 \text{ MeV}$$

$$m_\nu \sim 0.1 \text{ eV}$$

$$\alpha = \frac{\mu}{M} \sim 10^{-7}$$

# Spontaneous Inverse seesaw

To generate the **inverse seesaw** scheme we need to add **2 complex scalars**

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

$$m_D = \frac{y_L v_h}{\sqrt{2}}, \quad M = \frac{y_S v_S}{\sqrt{2}}, \quad \text{and} \quad \mu = \frac{y_X v_X}{\sqrt{2}}$$

# Spontaneous Inverse seesaw

To generate the **inverse seesaw** scheme we need to add **2 complex scalars**

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

$$v_S > 50 \text{ TeV} \quad v_X > 5 \text{ MeV}$$

# Spontaneous Inverse seesaw

But the **charge assignments** do not follow the typical one of the ISS

	$L$	$N_1$	$N_2$	$S$	$X$
$SU(2)_L$	2	1	1	1	1
$U(1)_Y$	1/2	0	0	0	0
$U(1)_I$	1	-1	$x$	$1 - x$	$2x$

$$x = 3/5$$

$$\mathcal{L} = -y_L \bar{L} H N_1^c - y_S S^\dagger \bar{N}_2 N_1^c - \frac{y_X}{2} X^\dagger \bar{N}_2^c N_2 + h.c.$$

# Scalar potential

The **assignment** fixes the potential

$$\omega = \frac{v_X}{v_S}$$

$$V_{\text{scalar}} = V_{XS} + V_{HXS} + V_I$$

$$V_I = \lambda_{\text{cp}} e^{i\delta} X S^{\dagger 3} + h.c.$$

$$S = \frac{v_S e^{i\theta} + \sigma_S + i\chi_S}{\sqrt{2}}$$

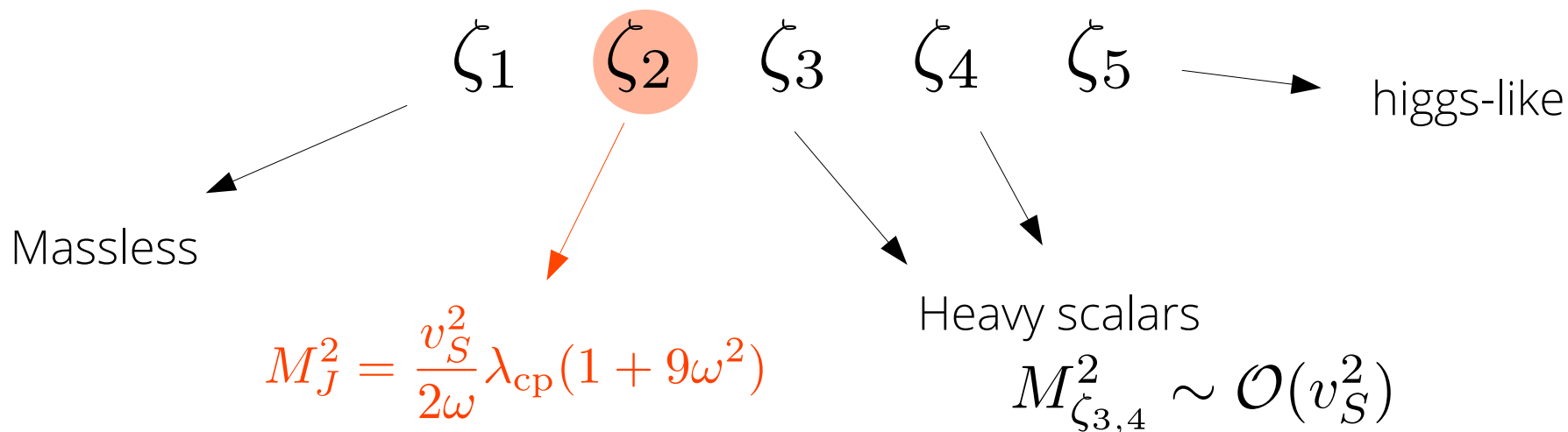
$$X = \frac{v_X e^{i\tau} + \sigma_X + i\chi_X}{\sqrt{2}}$$

The tadpole equations relate the CP phases:  $\tau = 3\theta - \delta - \pi$

# Mass spectrum

$$\omega = \frac{v_X}{v_S}$$

Now we have 5 spin-0 fields:      4 related to L breaking  
1 related to EW breaking



# Majoron DM stability

The only candidate is the *lightest massive scalar* i.e.  $\zeta_2 = J_{\text{DM}}$

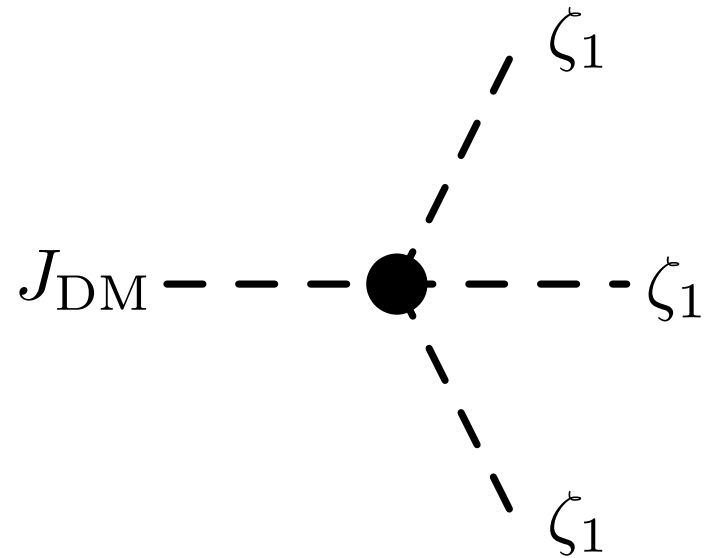
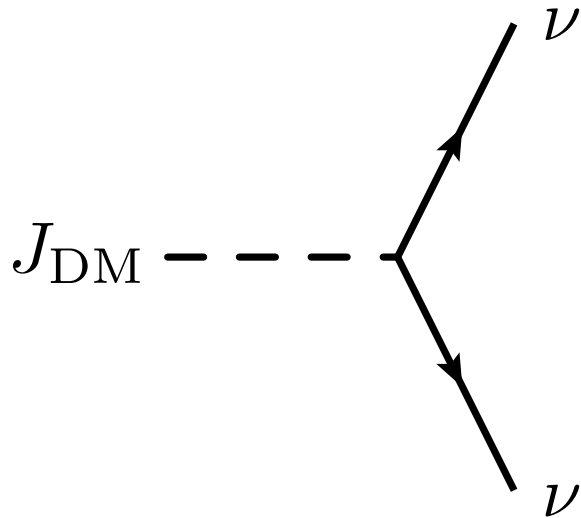
We still has to satisfy the stability condition:

$$\Gamma_{\text{DM}} < 10^{-52} \text{ GeV}$$



# Decay modes

There are potentially dangerous decay modes:



# Decay into neutrinos

$$\alpha = \frac{\mu}{M} \sim 10^{-7}$$

The decay rate vanishes for:

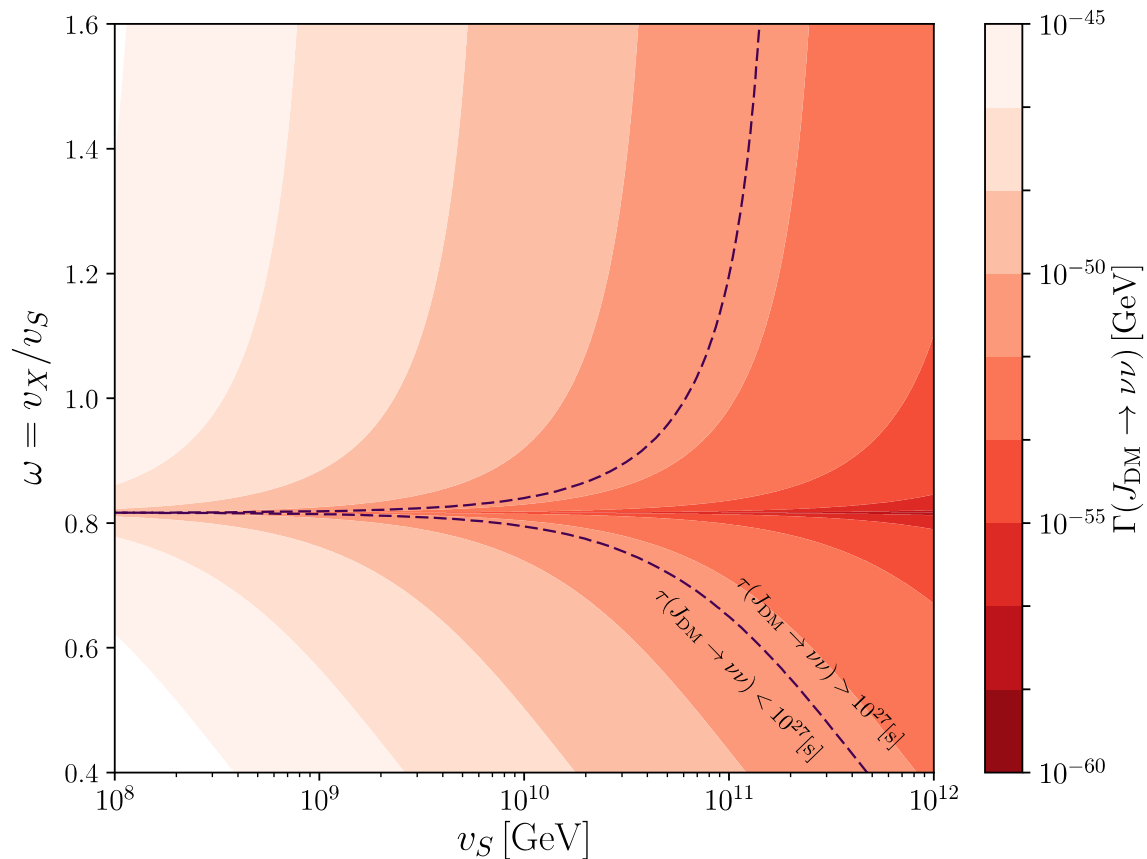
$$\omega_0 = \sqrt{2/3}$$

$$\Gamma_\nu = \Gamma_{0\nu}(\omega_0) 4\alpha^2$$

$$\Gamma_{0\nu}(\omega_0) \simeq 10^{-40} \text{ GeV} \left( \frac{m_\nu}{0.1 \text{ eV}} \right)^2 \left( \frac{M_J}{1 \text{ keV}} \right) \left( \frac{v_S}{100 \text{ TeV}} \right)^{-2}$$

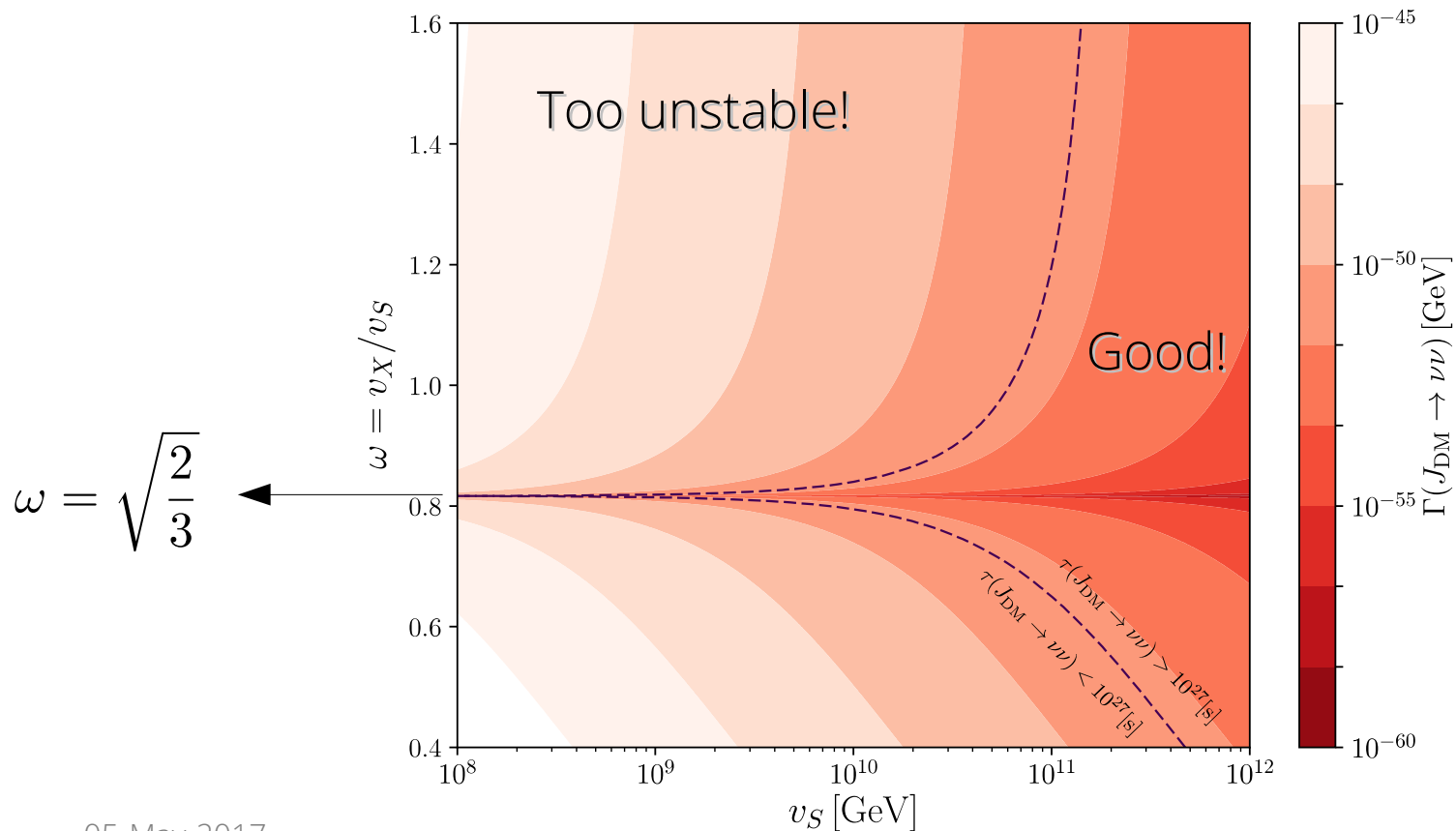
# Decay into neutrinos

$$J_{\text{DM}} \rightarrow \nu\nu$$



# Decay into neutrinos

$$J_{\text{DM}} \rightarrow \nu\nu$$



Stability thanks to  
vev alignment

# Decay into scalars

$$J_{\text{DM}} \rightarrow \zeta' \text{'s}$$

Without a protective symmetry, this channel is not suppressed

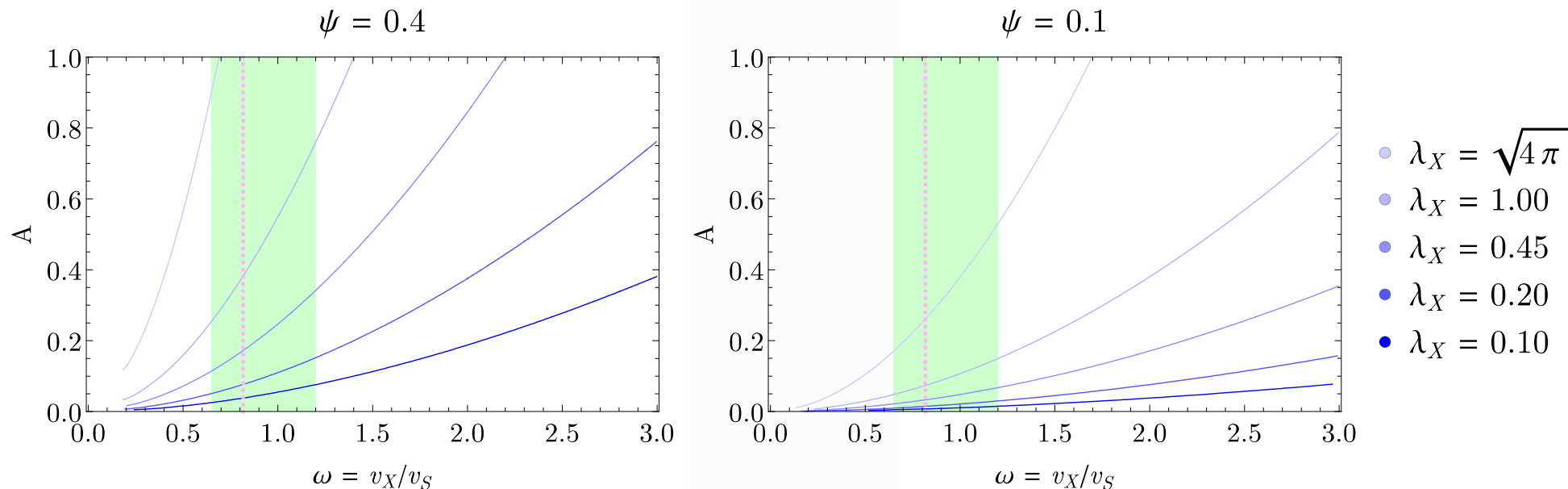
However we can find the parameter space where the **mode vanishes**

The diagram illustrates the decay of Majoron dark matter ( $J_{\text{DM}}$ ) into scalars ( $\zeta_1$ ). It shows an equality between two expressions:

- Left side:** A vertex (black dot) where a dashed line labeled  $J_{\text{DM}}$  enters from the left, and three dashed lines labeled  $\zeta_1$  exit to the right, top-right, and bottom-right. The vertex is labeled  $\lambda_{2111}^{\text{eff}}$ .
- Right side:** The sum of two terms:
  - First term:** A vertex (black dot) where a dashed line labeled  $J_{\text{DM}}$  enters from the left, and three dashed lines labeled  $\zeta_1$  exit to the right, top-right, and bottom-right. The vertex is labeled  $\lambda_{2111}$ .
  - Second term:** A sum over  $k=3,4,5$  of a diagram where a dashed line labeled  $J_{\text{DM}}$  enters from the left, and three dashed lines exit to the right: one labeled  $\zeta_1$  (top-right), one labeled  $\zeta_k$  (middle-right), and one labeled  $\zeta_1$  (bottom-right). The vertex is labeled  $\lambda_{12k}$  and  $\lambda_{11k}$ .

# Decay into scalars

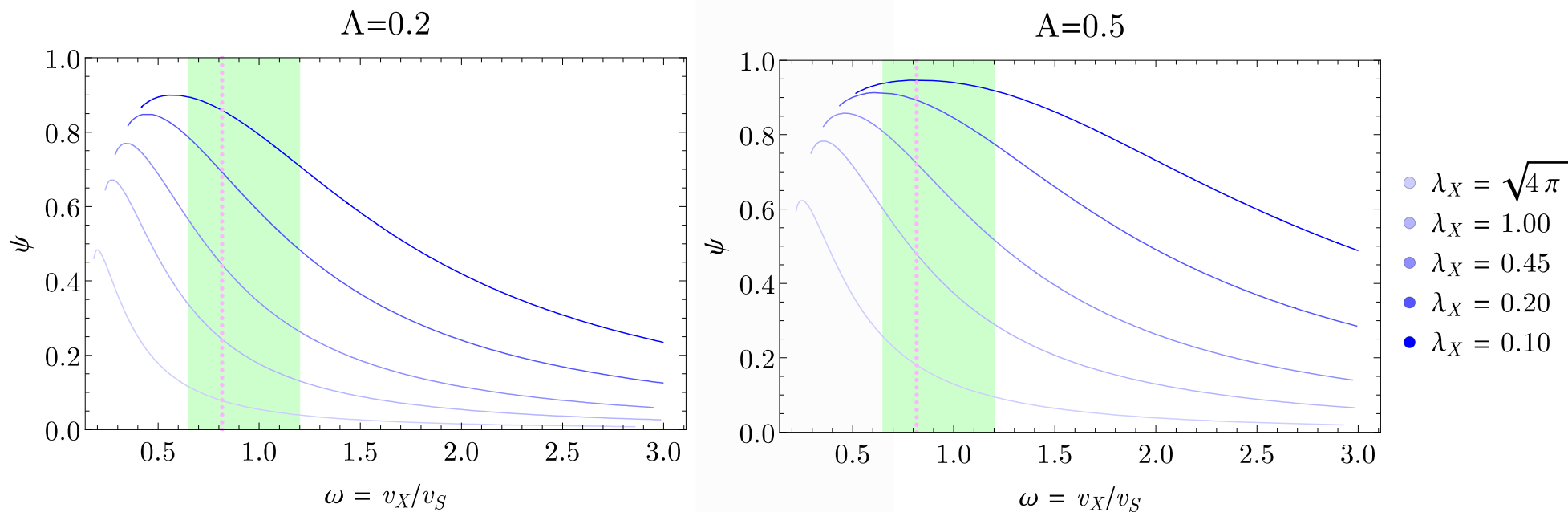
$$J_{\text{DM}} \rightarrow \zeta' \text{'s}$$



The interplay of different diagrams allows to vanish the decay mode

# Decay into scalars

$$J_{\text{DM}} \rightarrow \zeta' \text{'s}$$



There is a whole volume that satisfy this condition

# Conclusions

- The **spontaneous inverse seesaw** provides a well suited majoron DM candidate
- Our **majoron DM** is phenomenologically equivalent to the PNCB one
- The **vev alignment** has a relevant role in the DM stability



# Dark Matter Hunters

Digital resources for hunting the dark sector

[www.dmhunters.org](http://www.dmhunters.org)

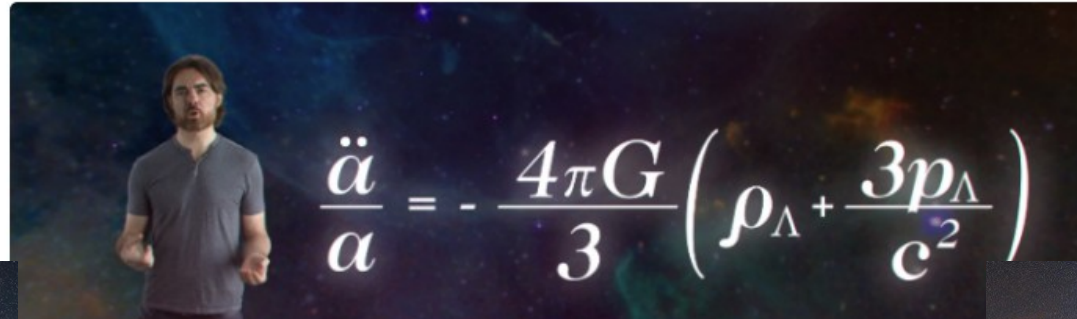
FOLLOW:



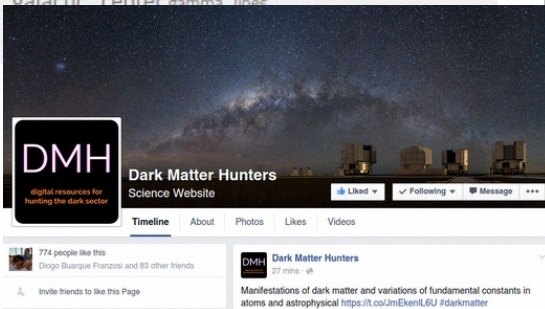
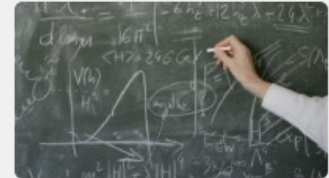
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# Sum Rules for Flavour Parameters

Martin Spinrath, NCTS (Taiwan)

Host: Joel Jones

Wednesday 3 May 2017 15:00 UTC

09:00 Colorado - 10:00 Mexico City, Lima, Bogotá - 11:00 New York - 12:00 Santiago, São Paulo, Buenos Aires - 16:00 London - 17:00 Brussels

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# Conclusions

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# Thanks!

# Extras

# Charge assignments

5 possible models

	$L$	$N_1$	$N_2$	$S$	$X$
$n = 1$	1	-1	1/7	6/7	2/7
$n = 2$	1	-1	1/3	2/3	2/3
$n = 3$	1	-1	3/5	2/5	6/5

$$m+n = 4$$

$$V_I = \lambda_{\text{cp}} e^{i\delta} X^m S^{\dagger n}$$

$$m+n = 3$$

	$L$	$N_1$	$N_2$	$S$	$X$
$n = 1$	1	-1	1/5	4/5	2/5
$n = 2$	1	-1	1/2	1/2	1

# The rest of the scalar potential

$$V_{SX} = -\mu_S^2 |S|^2 + \frac{\lambda_S}{4} |S|^4 - \mu_X^2 |X|^2 + \frac{\lambda_X}{4} |X|^4 + \lambda_5 |S|^2 |X|^2 + V_I$$

$$V_{HSX} = -\mu_H^2 H^\dagger H + \frac{\lambda_H}{4} (H^\dagger H)^2 + \lambda_{HS} |S|^2 H^\dagger H + \lambda_{HX} |X|^2 H^\dagger H$$

# Mass spectrum

$$m_h^2 \simeq \frac{v_h^2}{2} \left\{ \frac{\lambda_H}{2} + 2 \left( \frac{\lambda_{HX}^2 \lambda_S + \lambda_{HS}^2 \lambda_X - 4\lambda_5 \lambda_{HS} \lambda_{HX}}{4\lambda_5^2 - \lambda_S \lambda_X} \right) \right\}$$

$$M_{\zeta_3}^2 \simeq \frac{v_S^2}{2} \left( \frac{-A + A\psi + 2\lambda_X \omega \psi}{2\psi} \right)$$

$$M_{\zeta_4}^2 \simeq \frac{v_S^2}{2} \left( \frac{A + A\psi + 2\lambda_X \omega \psi}{2\psi} \right)$$

$$\lambda_S = A + \lambda_X \omega^2$$

$$\lambda_5 = -A \left( \frac{\sqrt{1 - \psi^2}}{4\omega\psi} \right)$$



# Numerology

Parameter	Value
$M$	100 TeV
$\mu$	10 MeV
$m_D$	10 GeV
$v_S$	$10^8 - 10^{12}$ GeV
$\omega$	0.4 – 1.6

$$\lambda_{\text{cp}} \simeq \frac{M_J^2}{v_S^2} < 10^{-22}$$